

# Chercheuse en sécurité informatique



Comment la société  
me voit



Comment on me voit quand  
j'explique mes idées



Comment l'Etat me voit



Comment je me sens quand  
j'attaque un chiffrement



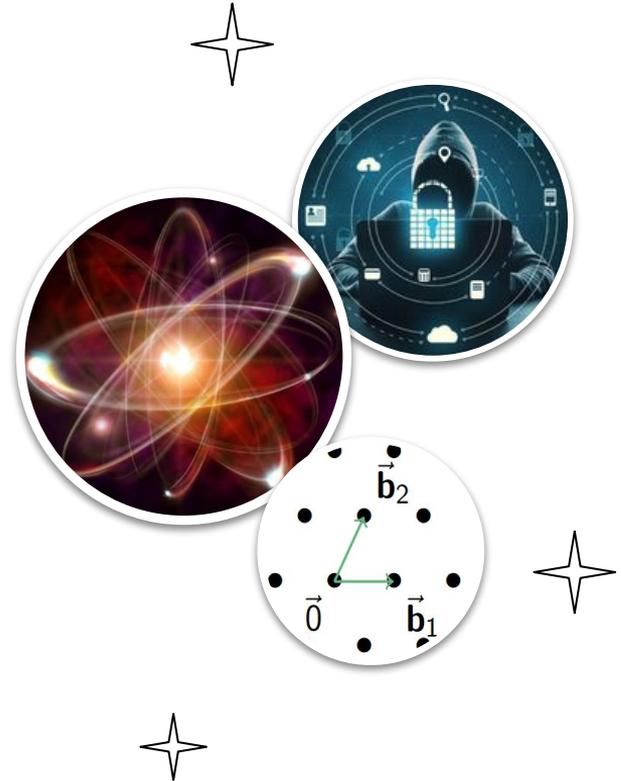
Comment mon copain me voit  
quand je suis en télétravail



Ce que je fais vraiment

# Cryptanalyse quantique des lattices

Dr. Johanna Loyer



52 av. J.C.



# Chiffre de César

Chiffrer

A → B

B → C

C → D

...

Y → Z

Z → A

PREPAREZ LE PIEGE  
SUR LA COLLINE  
D'ALESIA

Déchiffrer

A → Z

B → A

C → B

...

Y → W

Z → Y

QSFQBSFA MF QJFHF  
TVS MB DPMMJOF  
E'BMFTJB



# Chiffre de César

Chiffrer

A → B

B → C

C → D

...

Y → Z

Z → A

Déchiffrer

A → Z

B → A

C → B

...

Y → W

Z → Y

PVQT, QBT TJ  
TFDVSJTF RVF DB !



# Chiffre de César

Chiffrer

A → B

B → C

C → D

...

Y → Z

Z → A

OUPS, PAS SI  
SECURISE QUE CA !

Déchiffrer

A → Z

B → A

C → B

...

Y → W

Z → Y

PVQT, QBT TJ  
TFDVSJTF RVF DB !





# Enigma

1939

- 83 - ADJ JNA -

LMHNX WEKLM UERDS EVHLC  
JSQOK VLDES ANEVT YEDGI  
ZQDOD RMDKG SXGSQ SHDQP  
VIEAP IENLI CLZCL LAGWC  
BJZD



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Cryptanalyse



# Enigma

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LMHNX WEKLM UERDS EVHLC  
JSQOK VLDES ANEVT YEDGI  
ZQDOD RMDKG SXGSQ SHDQP  
VIEAP IENLI CLZCL **HEIL**  
**HITLER**

Cryptanalyse



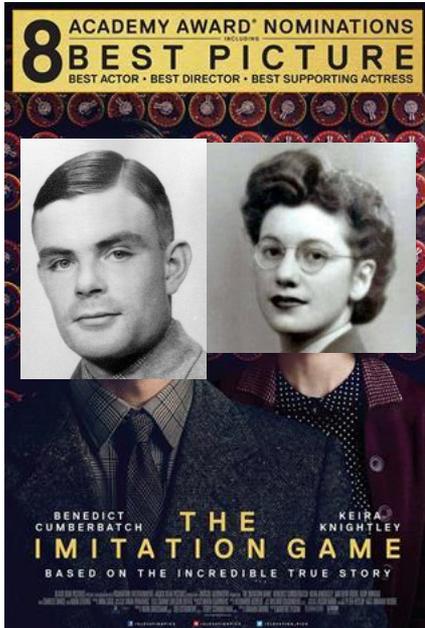
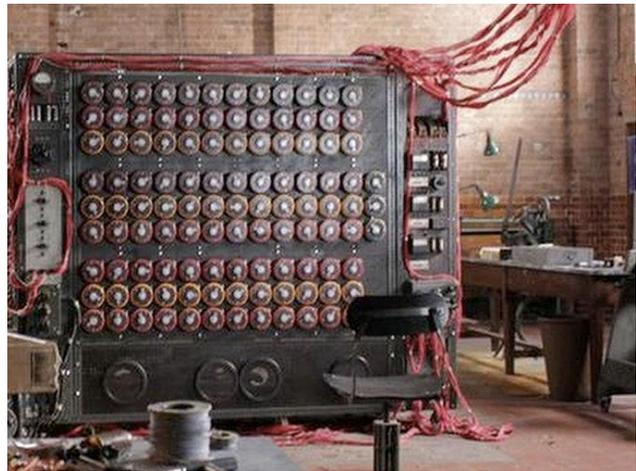
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## Cryptanalyse





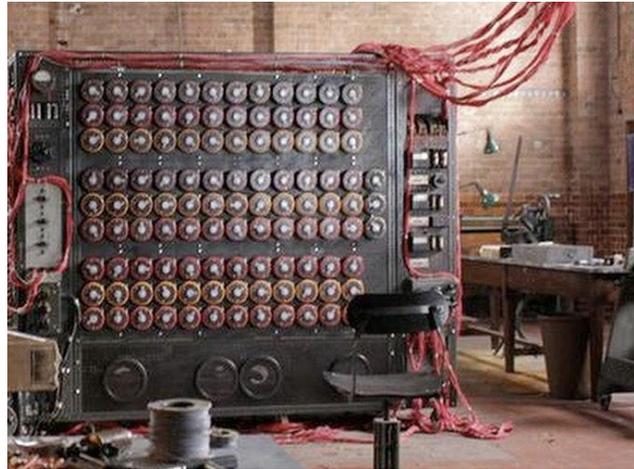
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1939

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 JSQQK VLDES ANEVT YEDGI  
 ZQDOD RMDKG SXGSQ SHDQP  
 VIEAP IENLI CLZCL **HEIL**  
**HITLER**

## Cryptanalyse



Années 1970



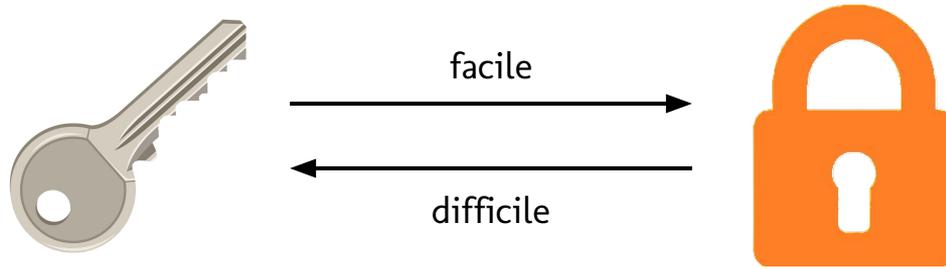
Années 1970



# Pourquoi la sécurité informatique est-elle importante ?



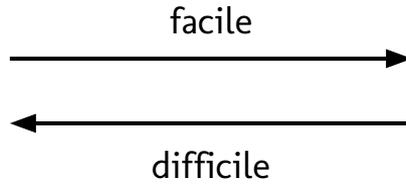
# Chiffrement asymétrique



# Chiffrement asymétrique



Nombres premiers  
P et Q



$P \times Q$



Rivest, Shamir & Adleman

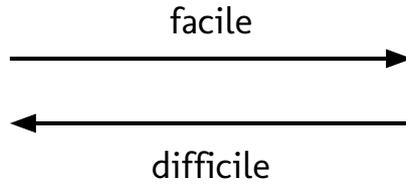
$$P \times Q =$$

7487869927382228767030641005652582376664116895591925942032312045821425380552073005291076958  
9310154430228567886782322253163986663671065974410591516257916784327030655524680115587855657622  
69415511054634086033391917807255228011912006081719185419030150337935853314471455278465677199388  
6634856241405809880117441029508975191737513326356386593323855753894172373033807560692526663128  
239234718590443206457755768522058106983374764382193706546199518762495507385546703190424412194  
646520350487376579137499225032384179194492563915431360553097163206866690722336841973631155010  
42878337123741086644394226378033905592006616040673005608191041617047062052006640741371629  
288703113244157939980609005142380531520757992544004840633308722004008246941614587623136992  
44427168410010234953322369230131008875207144178060016690500990949035506940693521719866602  
606841848144161385641366094783418163579176641469113458683986636271624156226808640075322348660  
856868239917652135854264247202737344360664539192915544469799363161283822017014838671695003776  
89640016034813328639089595188900543842473805635216548074511467632695923063570000124926420  
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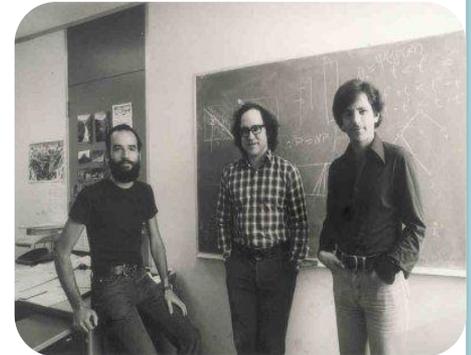
# Chiffrement asymétrique



Nombres premiers  
P et Q



$P \times Q$

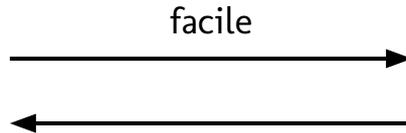


Rivest, Shamir & Adleman

# Chiffrement asymétrique



Nombres premiers  
P et Q



facile

~~difficile~~

facile avec un  
ordinateur quantique !



$P \times Q$

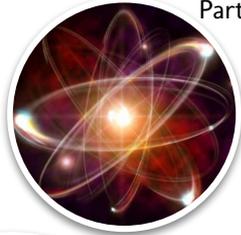


Ordi classique : 0 ou 1



Ordi quantique : 0 et 1  
**en même temps**

# Physique quantique



Particule quantique dans plusieurs états en même temps



Chat de Schrödinger



# Physique quantique



Particule quantique dans plusieurs états en même temps



Chat de Schrödinger



« Personne ne comprend vraiment la physique quantique. »

— Richard Feynman



# Qui veut construire un ordinateur quantique ?

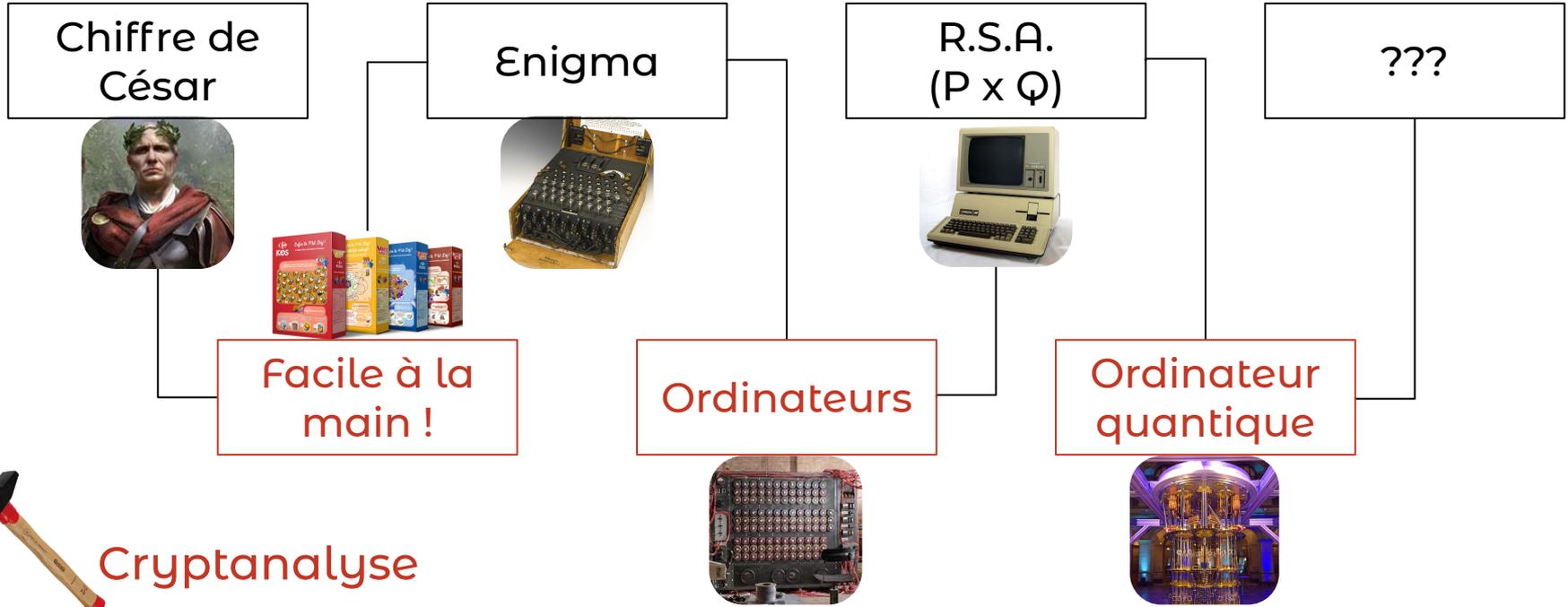


Edward Snowden

# Petit résumé jusqu'ici



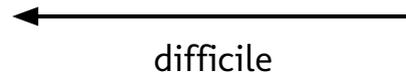
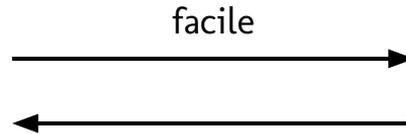
## Chiffrement



# Chiffrement “post-quantique”

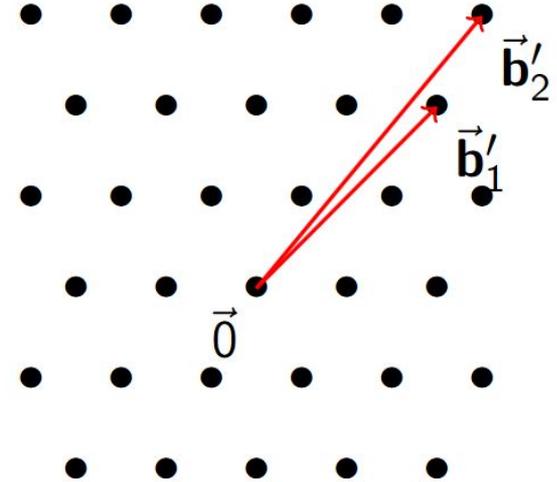
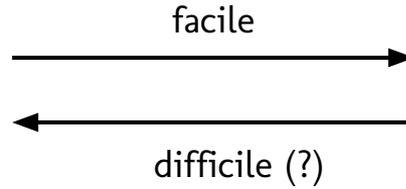
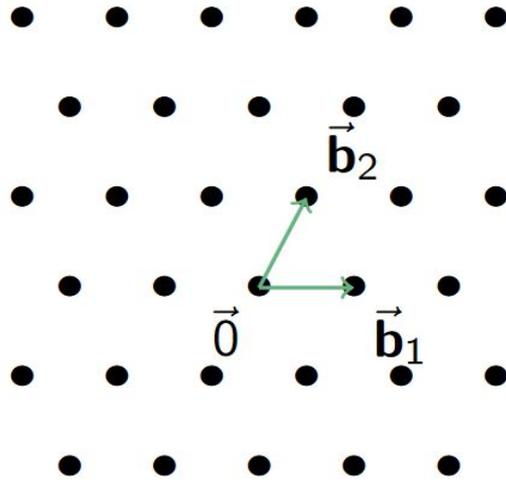


?



?

# Chiffrement "post-quantique"





# Chiffrement

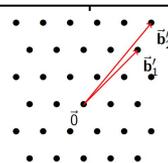
Enigma



R.S.A.  
( $P \times Q$ )



Lattices



Ordinateurs



Ordinateur  
quantique



???



Cryptanalyse



Les lattices sont-ils aussi  
sécurisés qu'on le croit ?



# Plan



**1**

Attaque sur les lattices

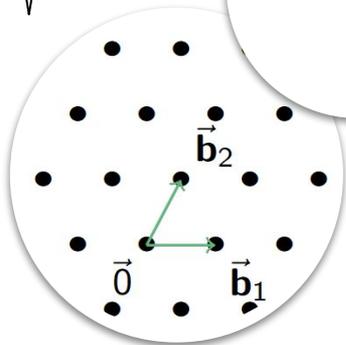
**2**

Amélioration de l'attaque

**3**

Mon attaque

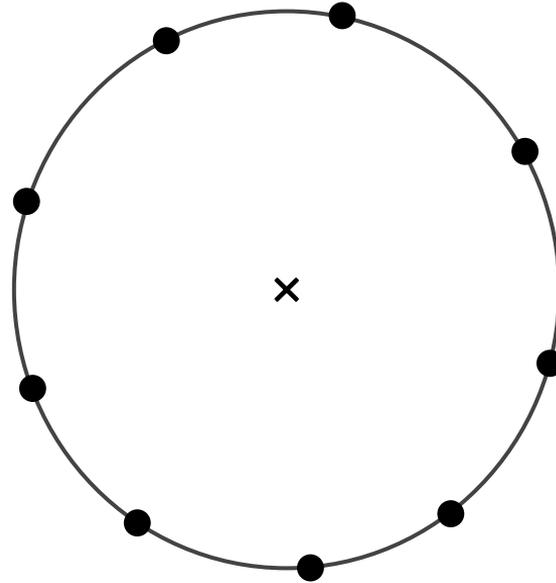




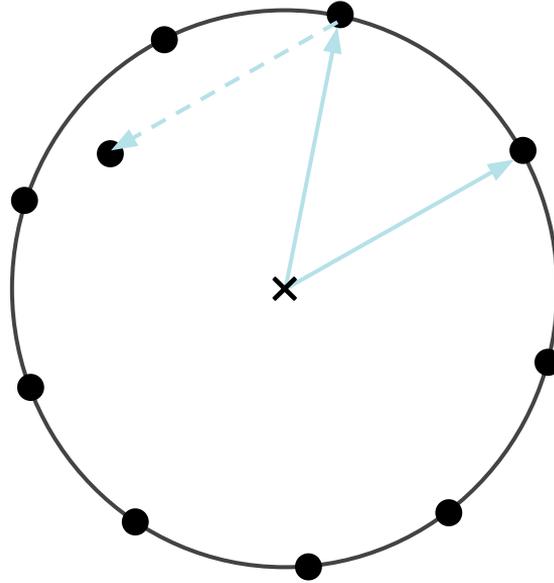
# Attaque sur les lattices

En combien de temps peut-on  
retrouver un petit vecteur ?

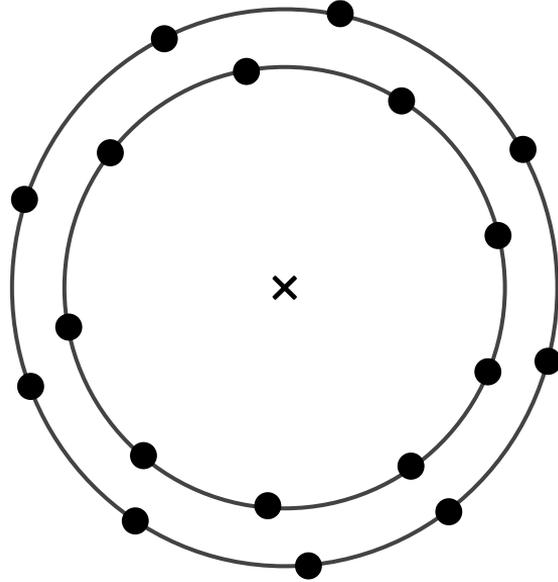
# Méthode du crible



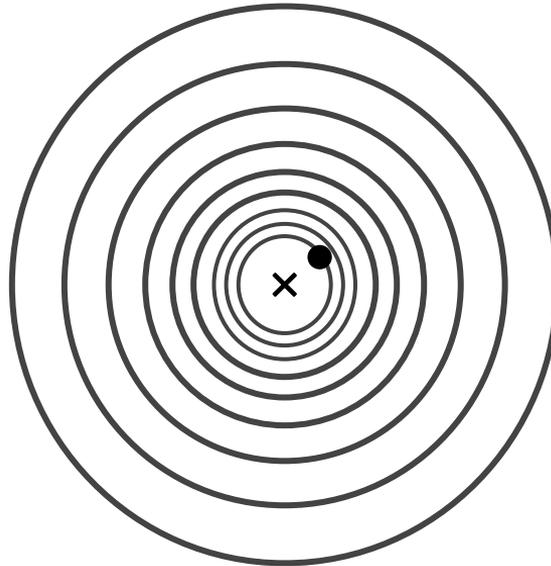
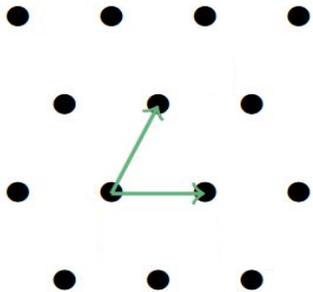
# Méthode du crible



# Méthode du crible



# Méthode du crible



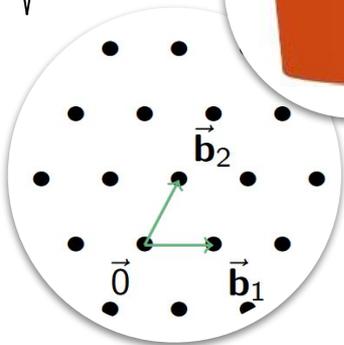
Temps de l'attaque :

$$10^{0.125d} \text{ opérations}$$

Meilleure attaque  $> 10^{39}$  :  
"Sécurisé"

En dimension  $d=308$  :

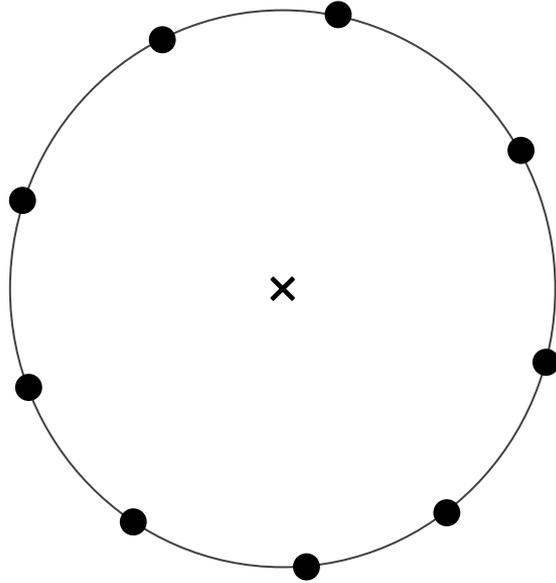
$$10^{0.125d} = 10^{39}$$



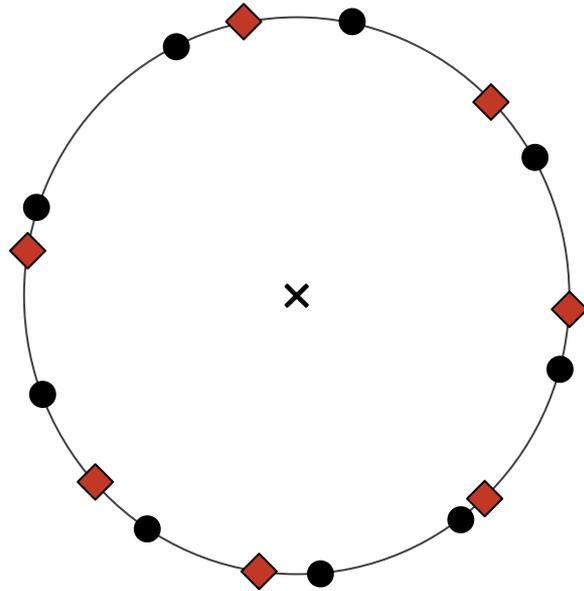
# Amélioration de l'attaque

Comment trouver les points proches  
plus rapidement ?

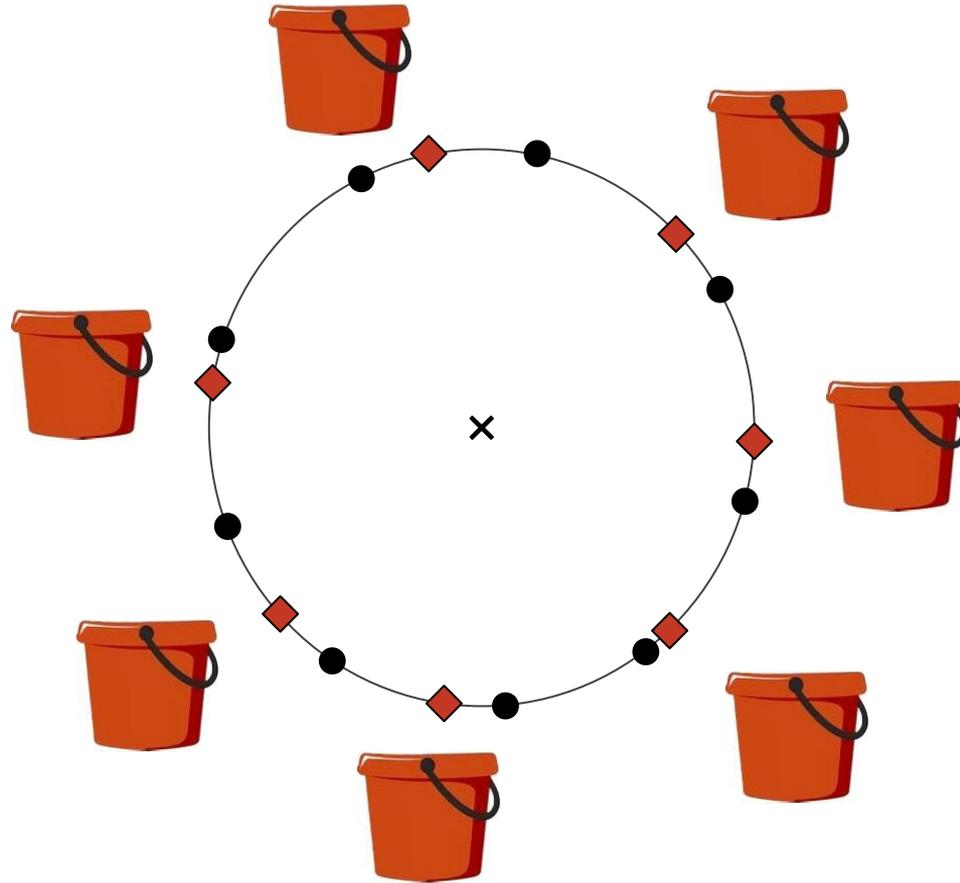
# Filtrage



# Filtrage

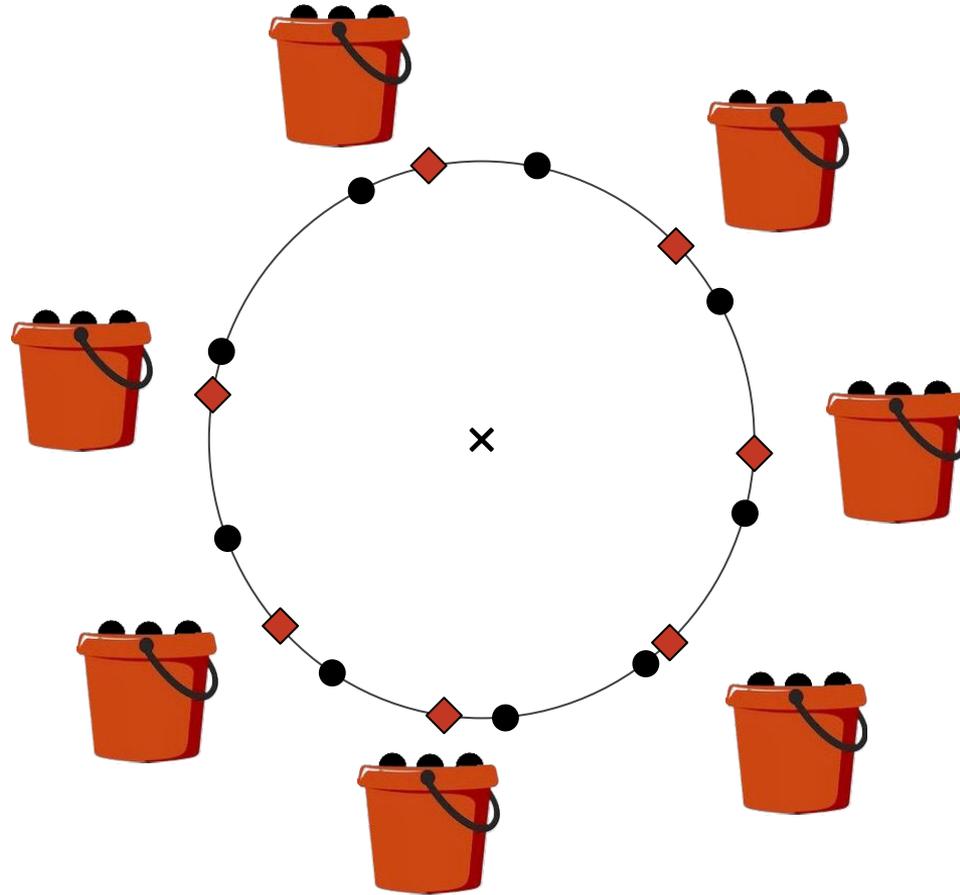


# Filtrage





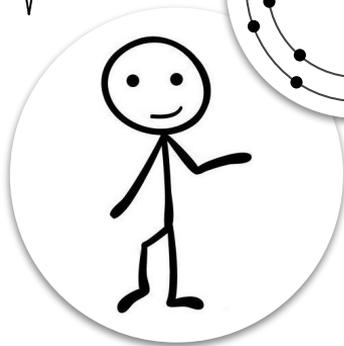
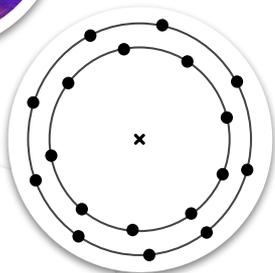
# Filtrage



# Méthode du crible avec filtrage

d = 500	Classique	Quantique
Sans filtrage	$10^{62}$	$10^{47}$
Avec filtrage 	$10^{44}$	$10^{40}$

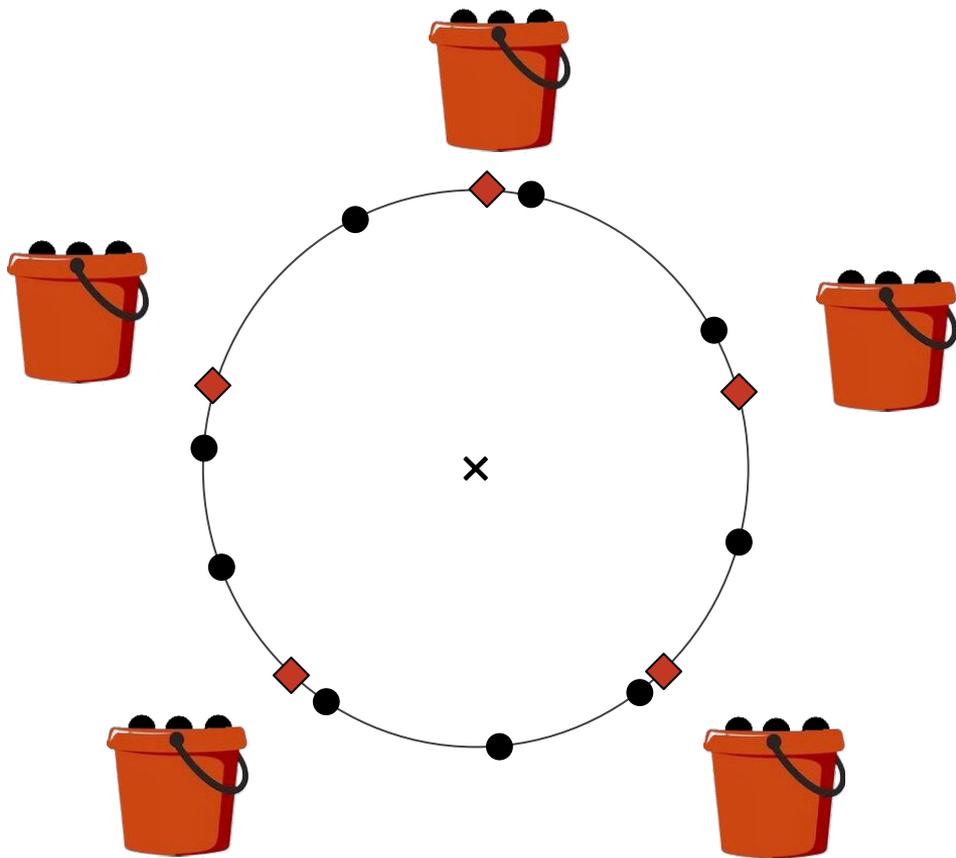
Nombre d'opérations des attaques  
>  $10^{39}$  "Sécurisé"



# Mon **attaque**

(avec Sticky en guest star)

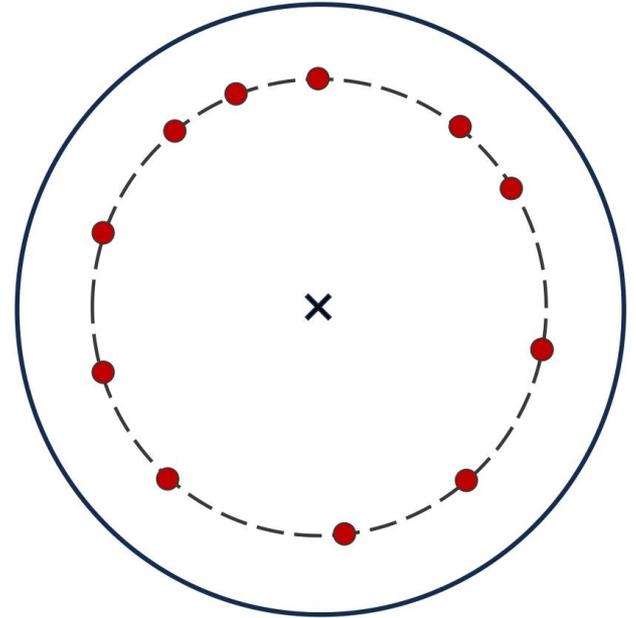




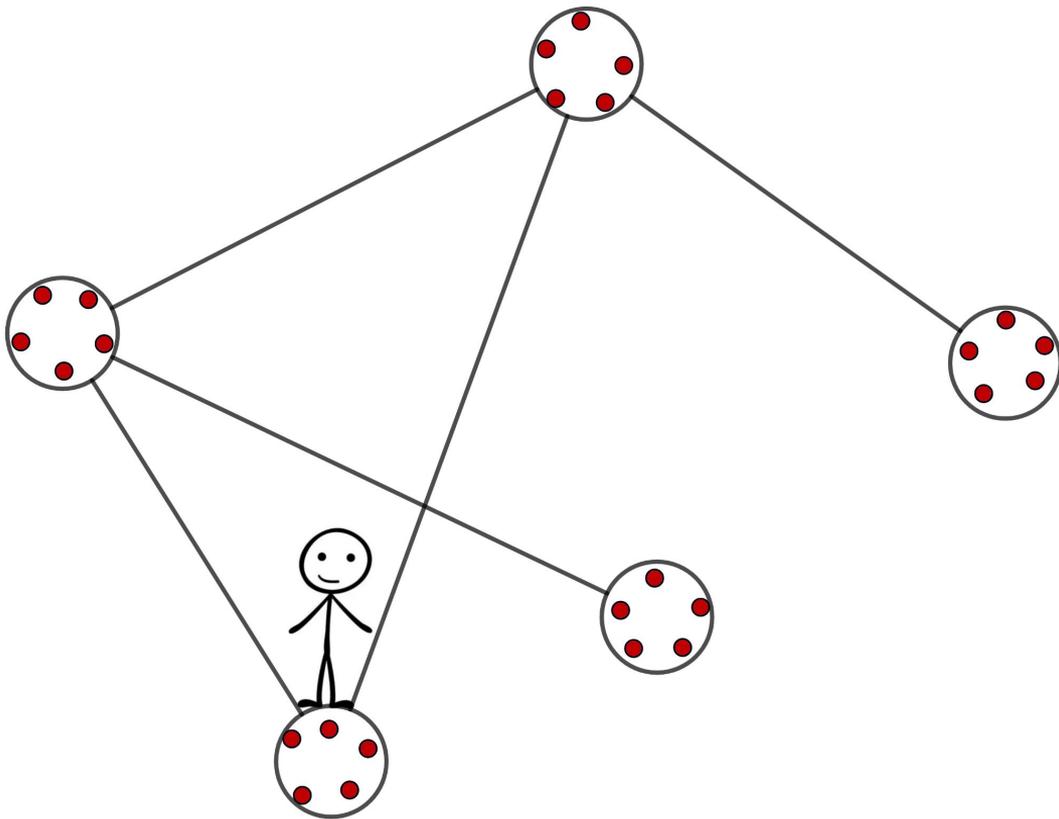
Objectif : Trouver 2 points proches dans



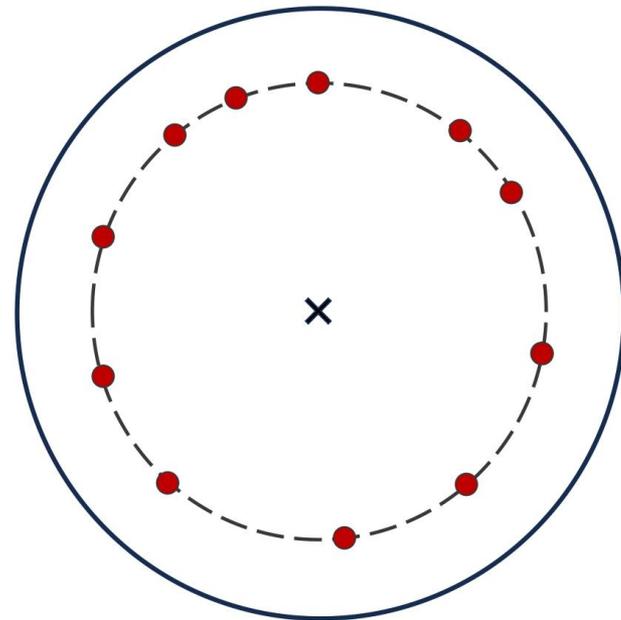
Objectif : Trouver 2 points proches dans



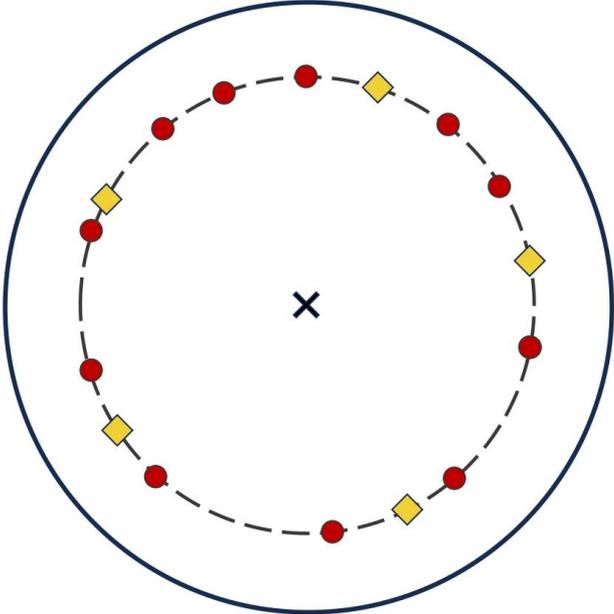
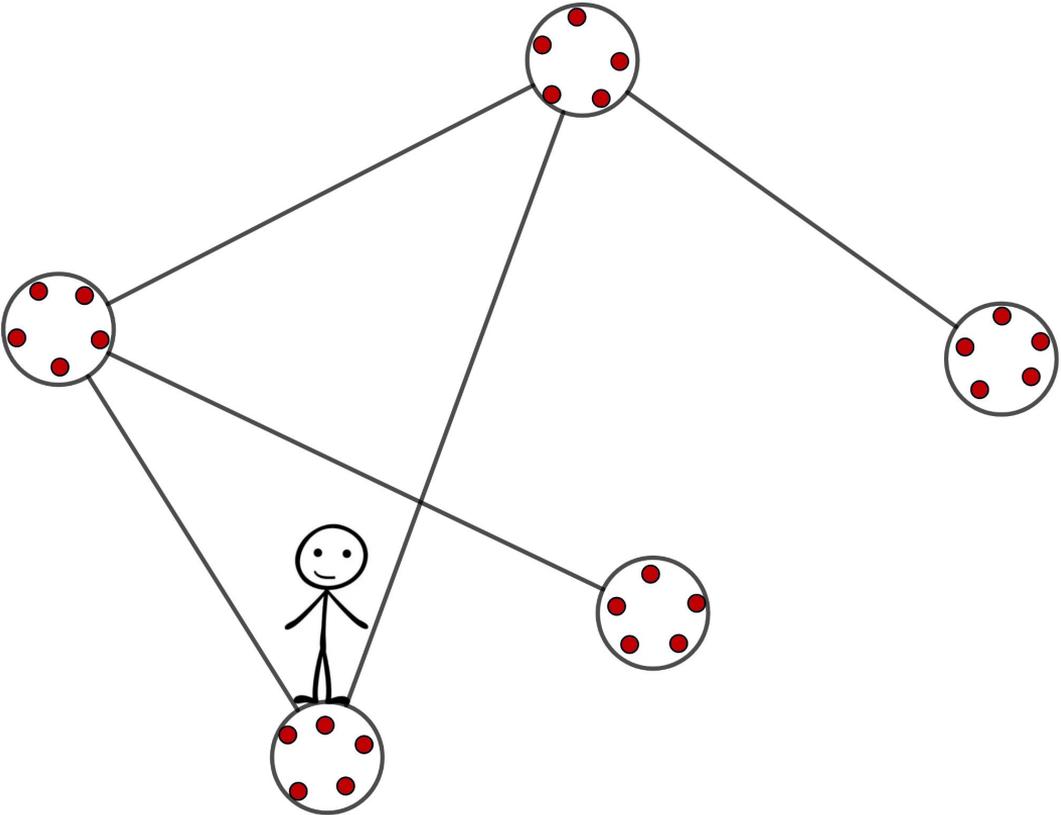
Objectif : Trouver 2 points proches dans



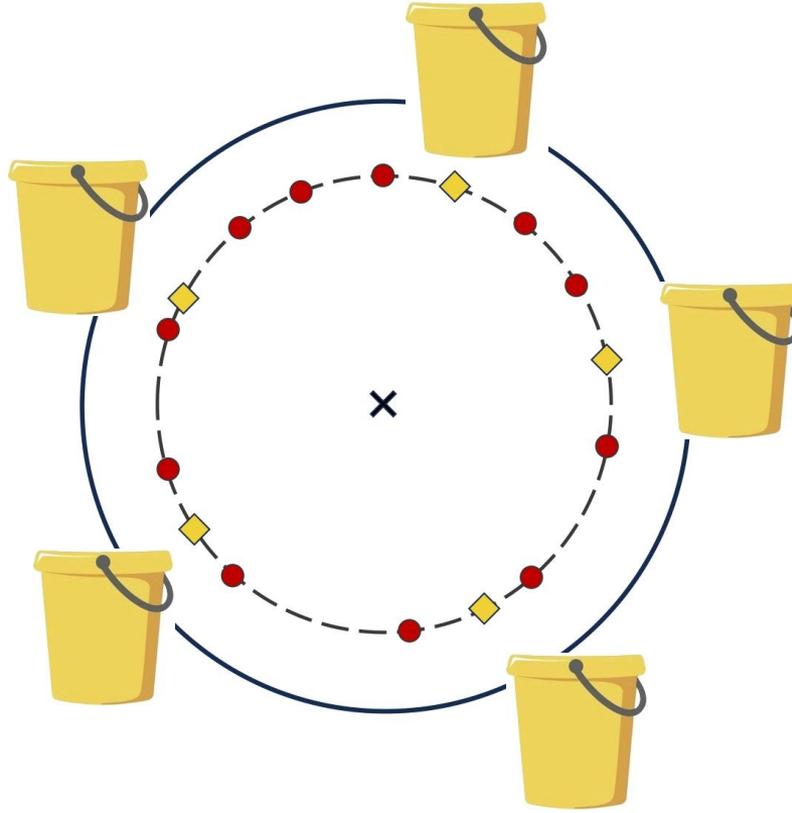
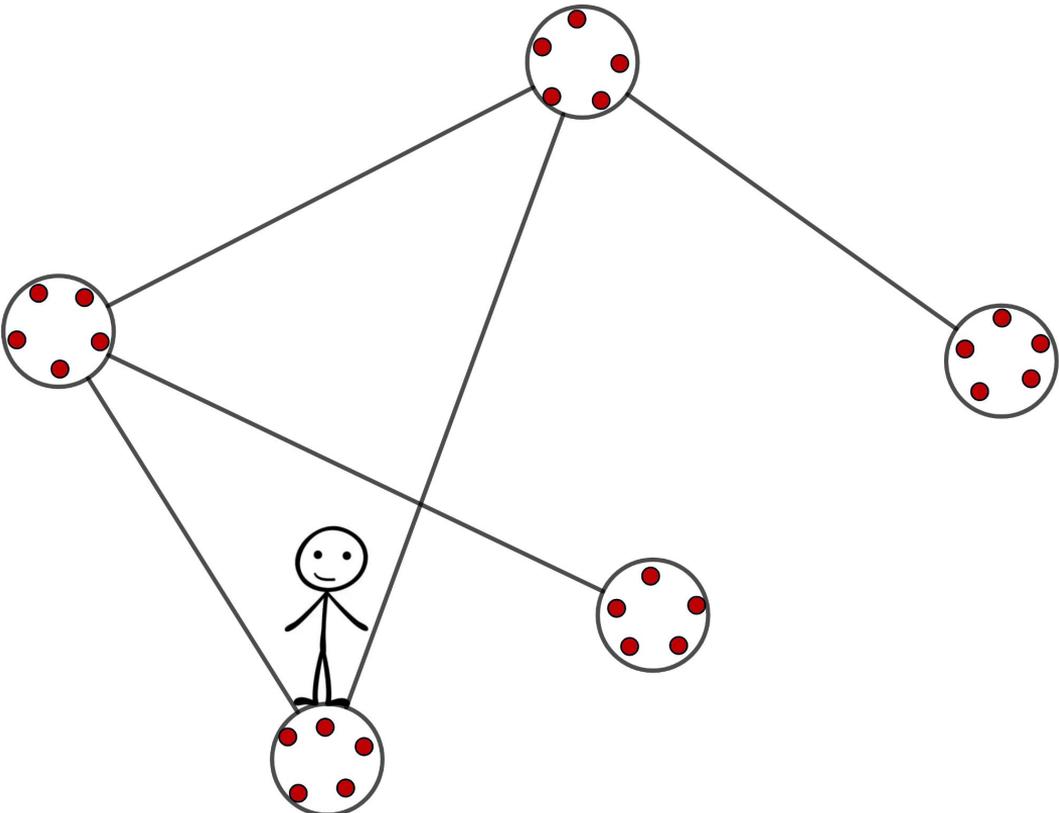
Zoom sur l'ensemble de points  
où se trouve Sticky



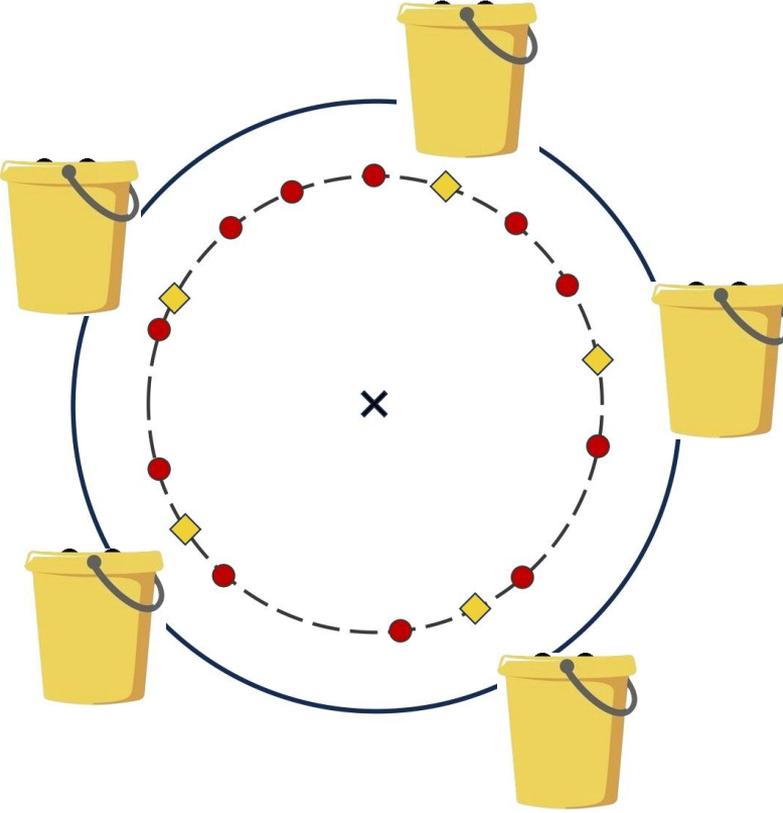
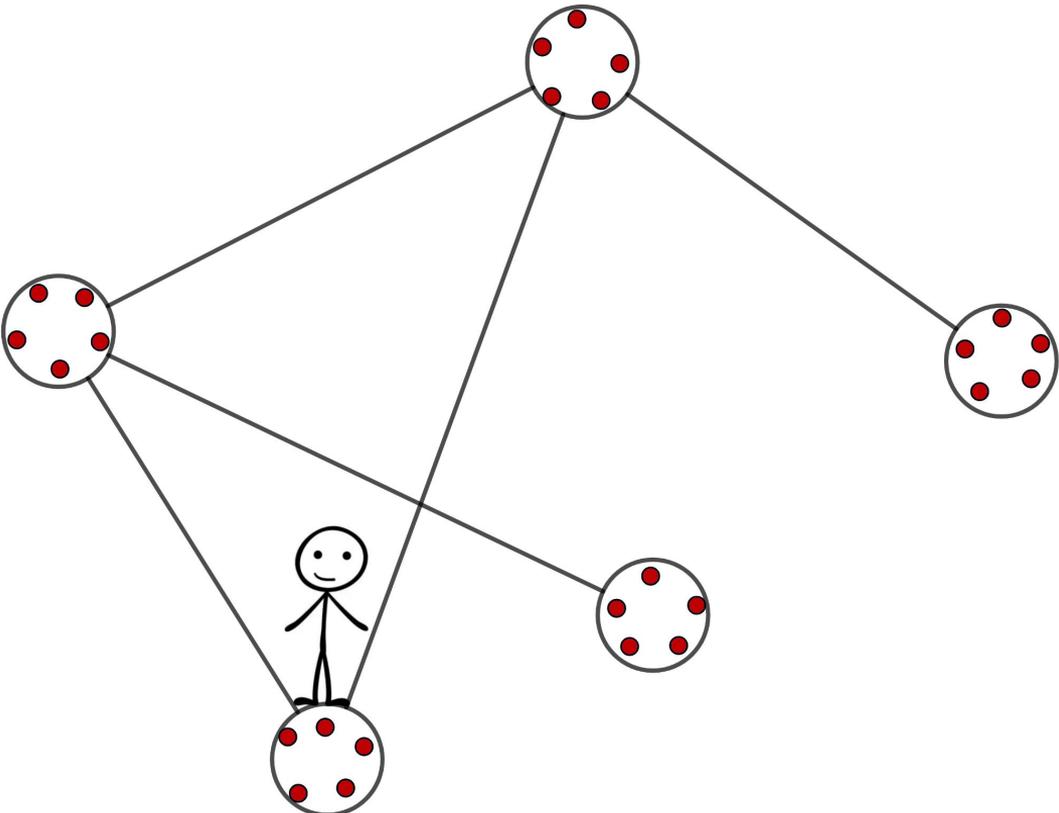
Objectif : Trouver 2 points proches dans



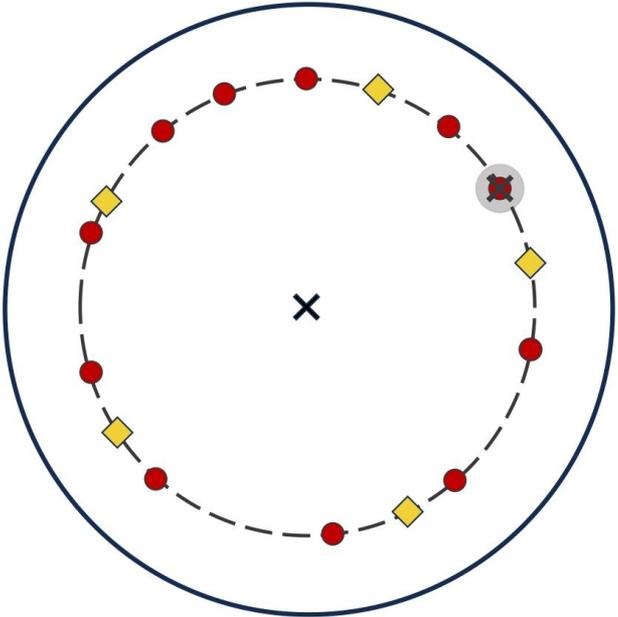
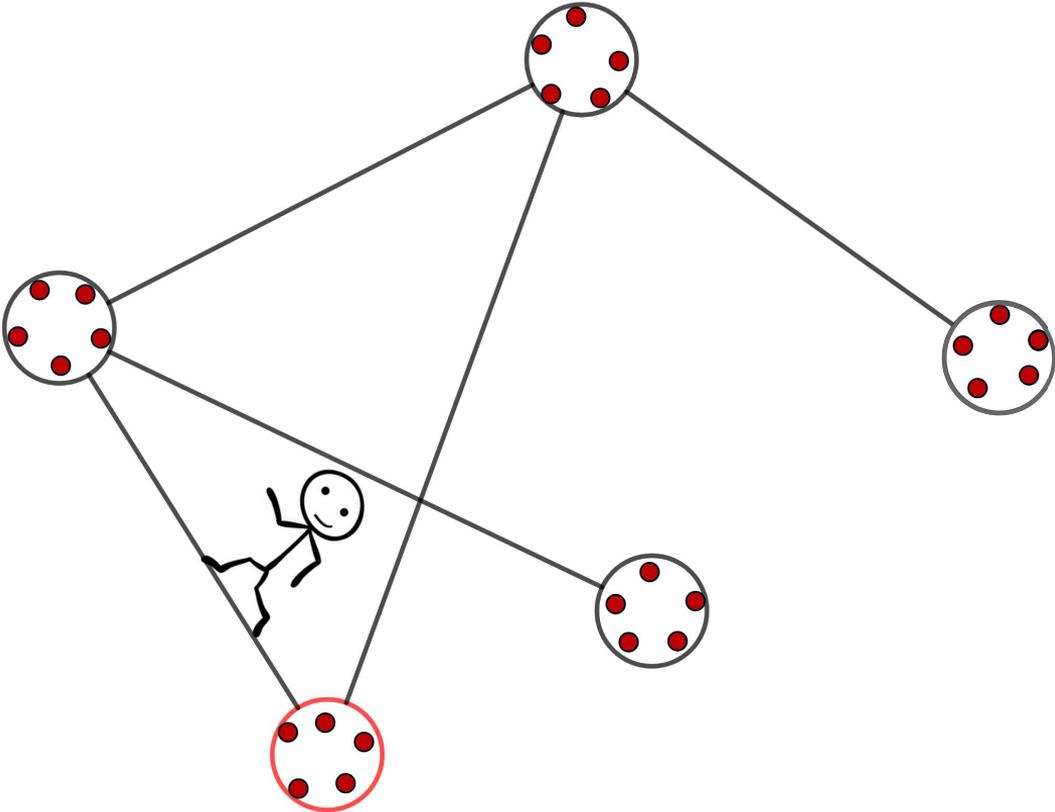
Objectif : Trouver 2 points proches dans



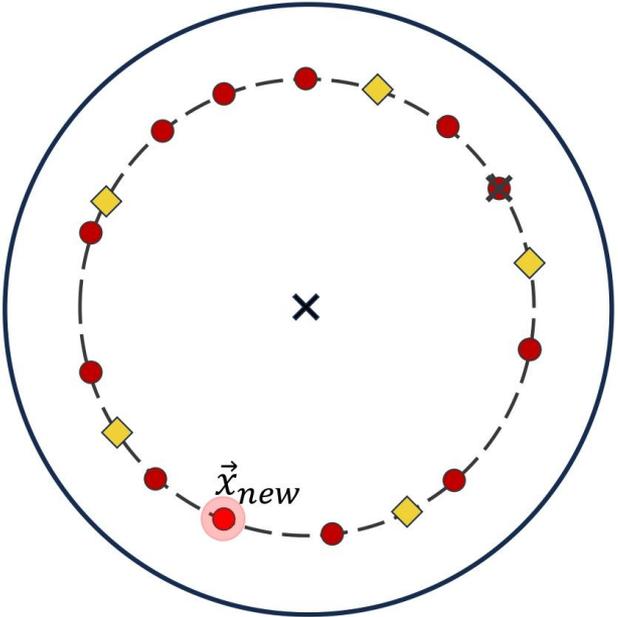
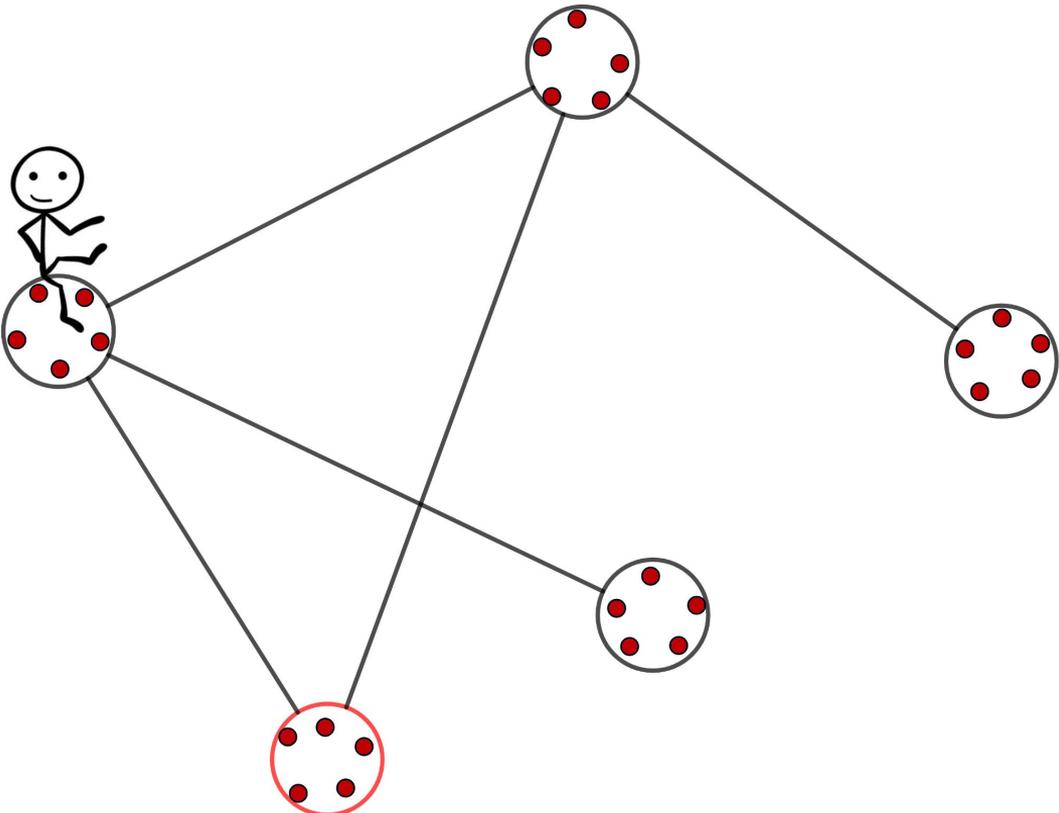
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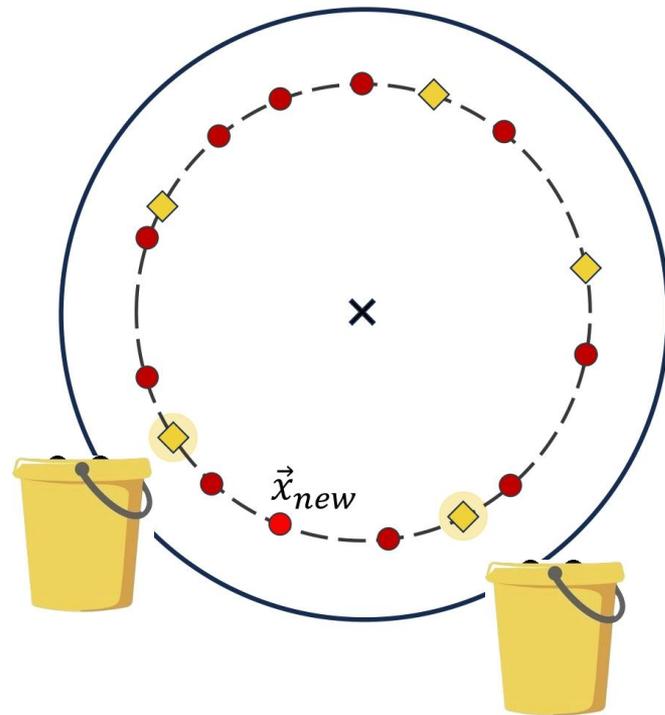
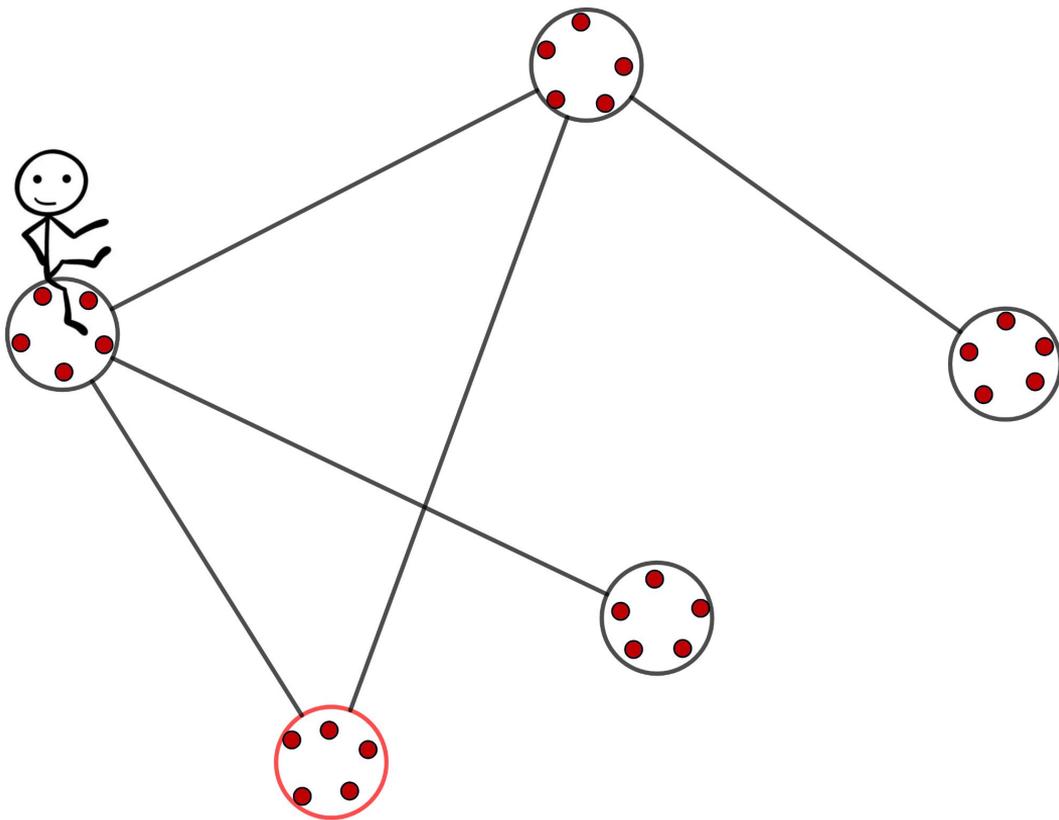
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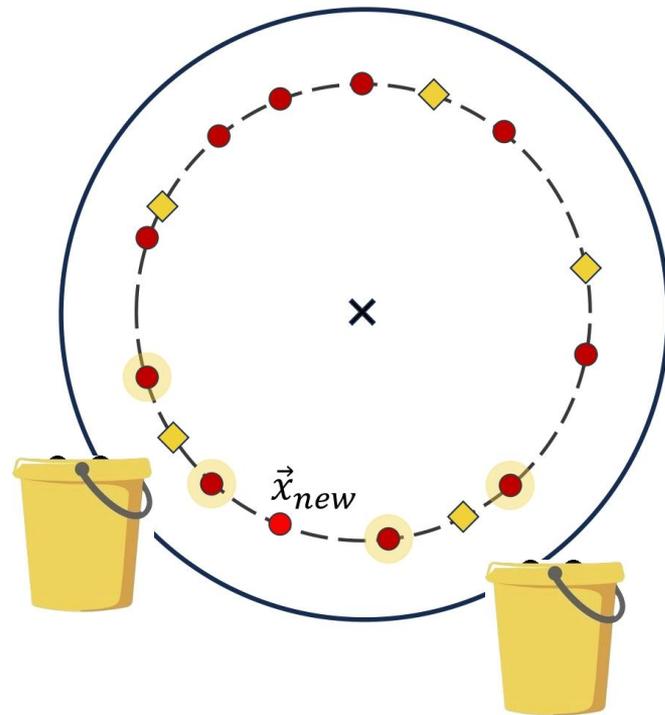
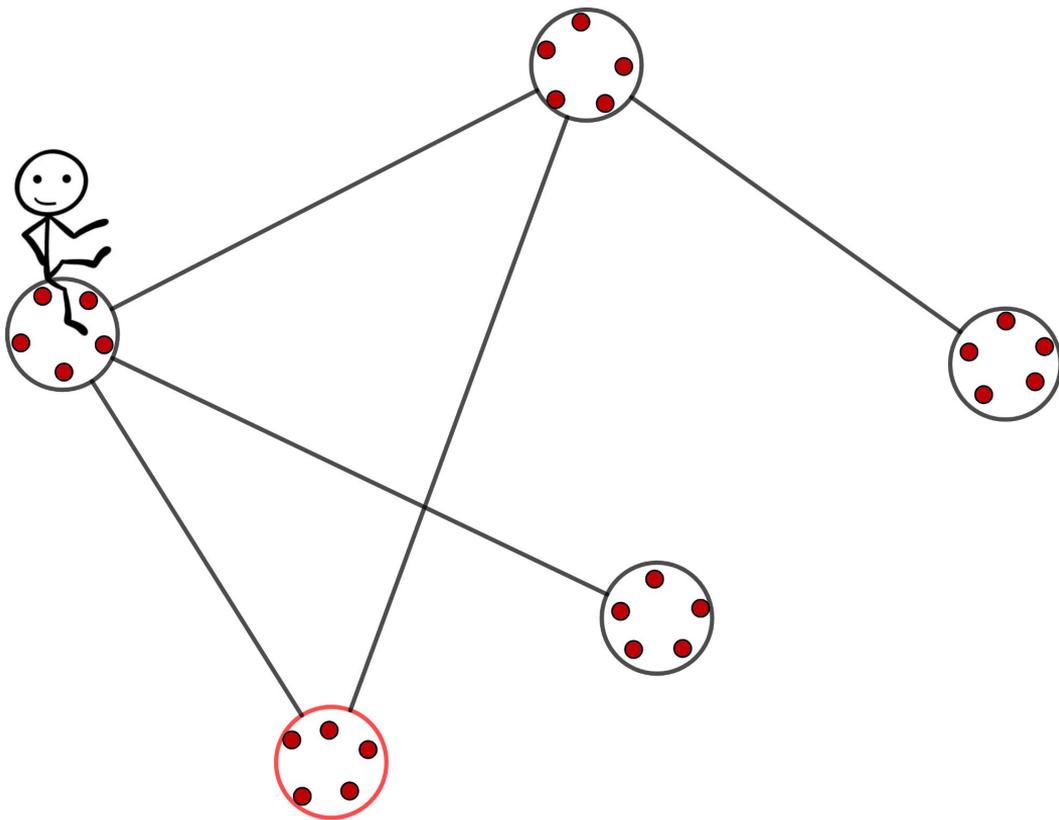
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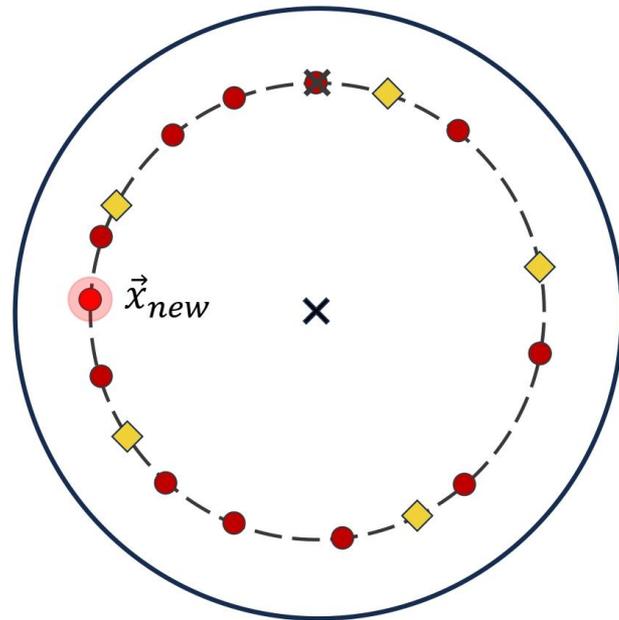
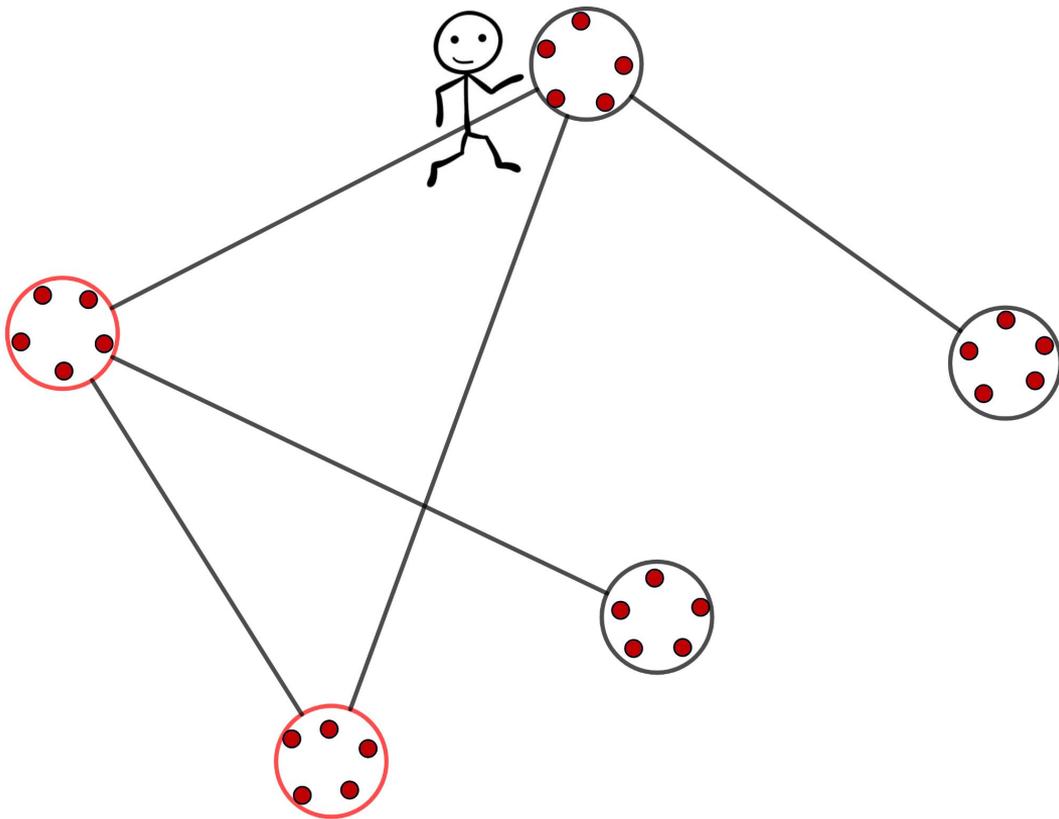
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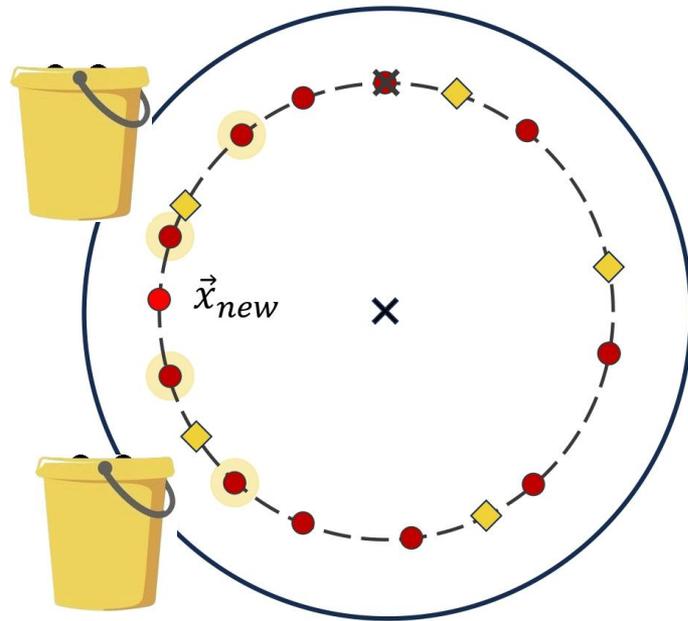
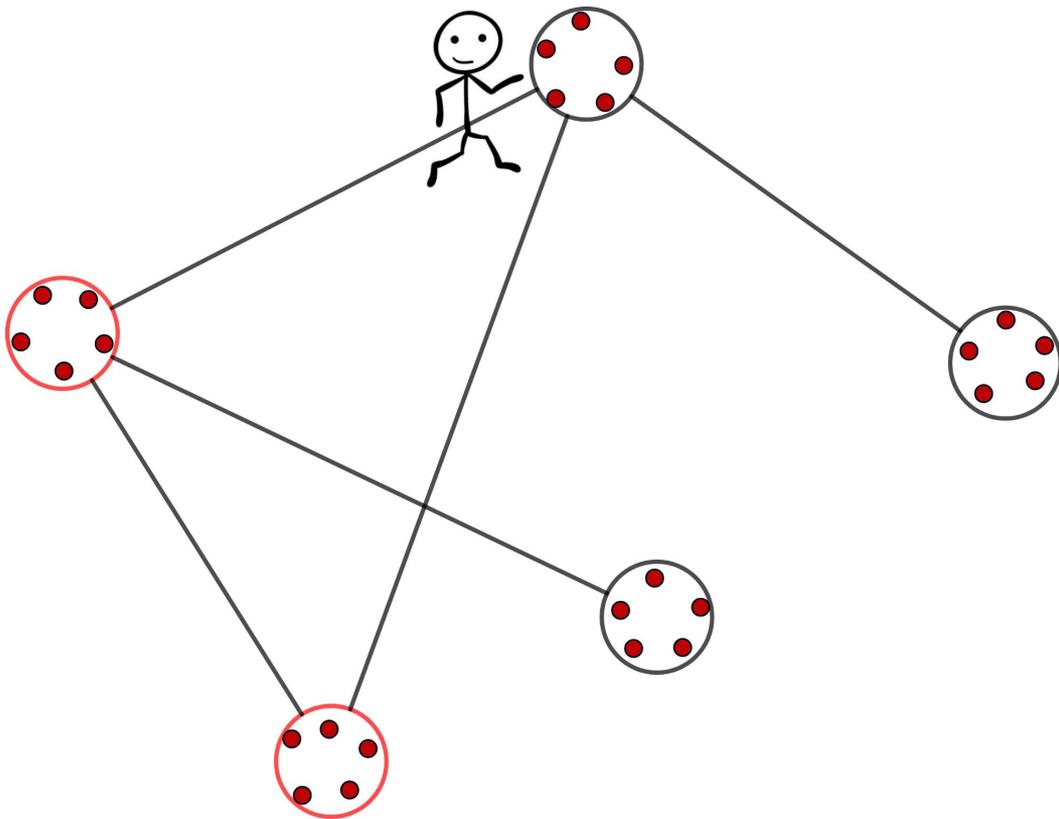
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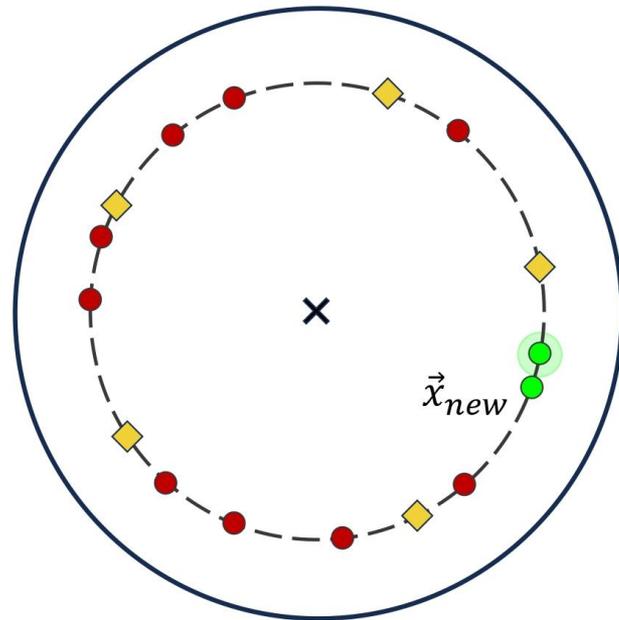
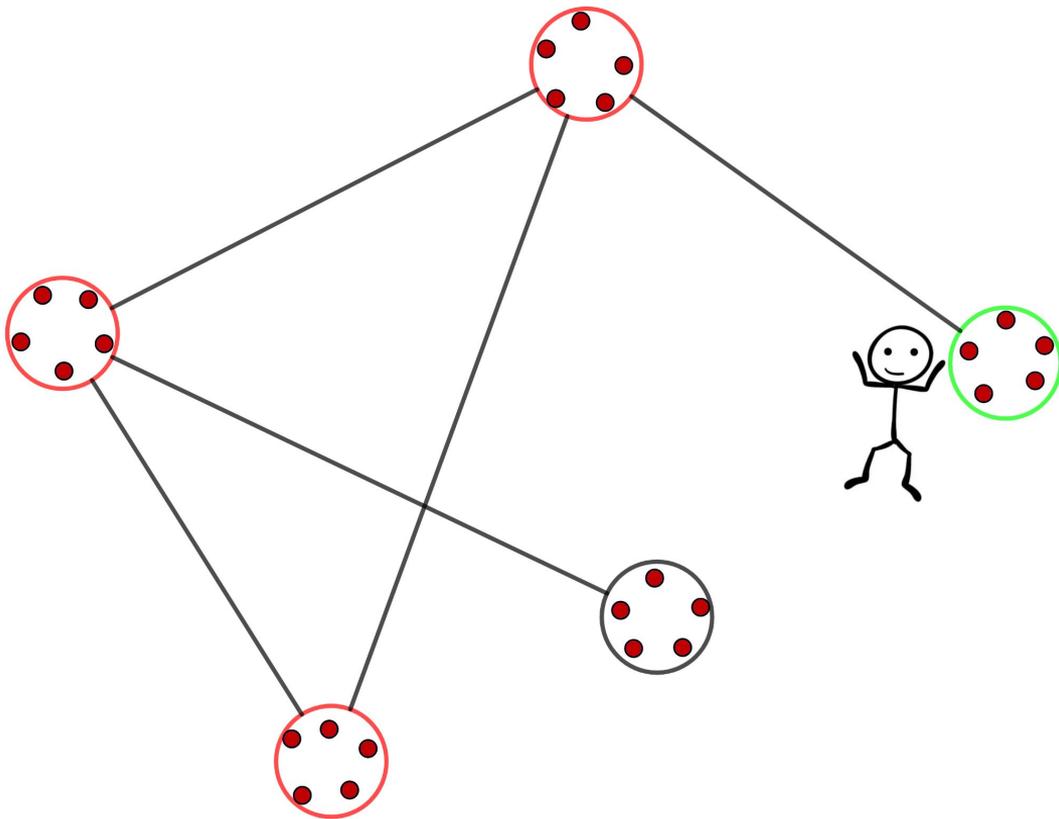
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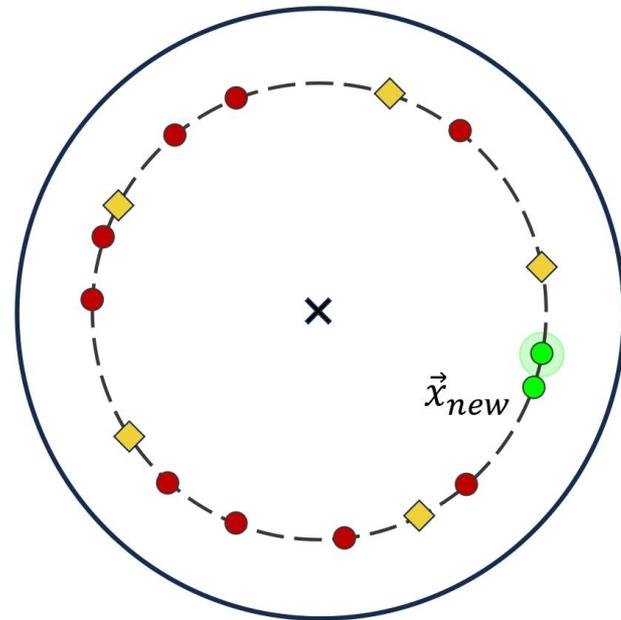
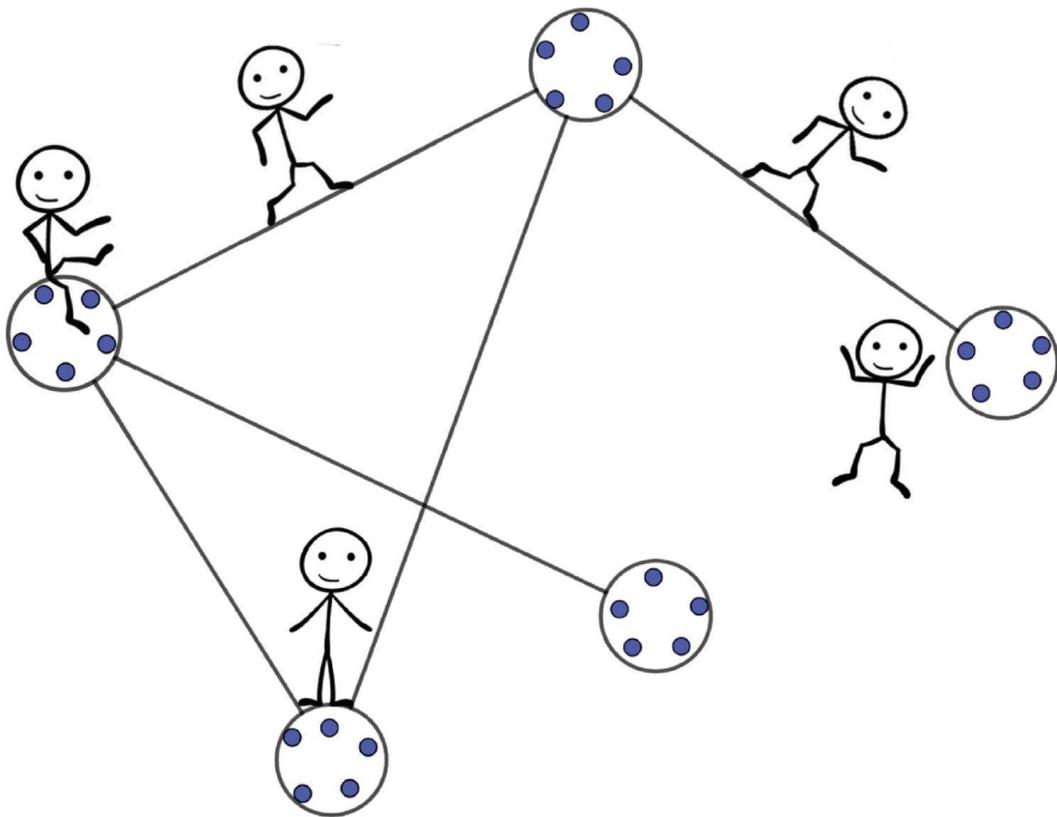
Objectif : Trouver 2 points proches dans



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Objectif : Trouver 2 points proches dans



# Attaques connues contre les lattices

d = 500	Classique	Quantique
Sans filtrage	$10^{62}$	$10^{47}$
Avec filtrage 	$10^{44}$	$10^{40}$
Marche quantique 	<del></del>	$10^{38}$



# Attaques connues contre les lattices

d = 500	Classique	Quantique
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Marche quantique 	<del></del>	$10^{38}$

$< 10^{39}$



# Cryptanalyse quantique des lattices

Dr. Johanna Loyer

